



# Honors Physics Study Guide

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## **Breakdown of Units**

\*\*topics discussed may vary between schools. The units in this guide are the main topics discussed in many physics courses.

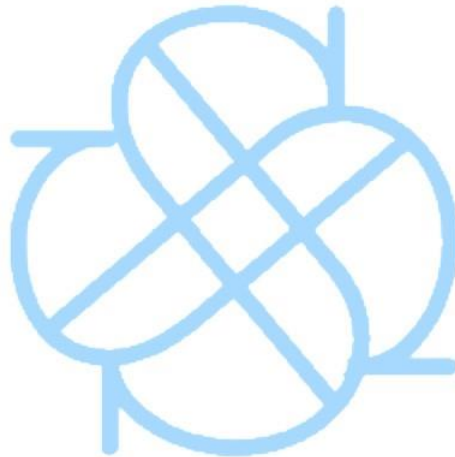
**Unit 1:** Kinematics (1D and 2D motion)

**Unit 2:** Newton's Laws of Motion

**Unit 3:** Circular Motion

**Unit 4:** Work and Energy

**Unit 5:** Electric Currents and Magnetism



# 1 Dimensional Motion

## Introduction to Speed and Velocity

### Key Equations:

Average speed = (distance)/(time)

Average velocity = (displacement)/(time)

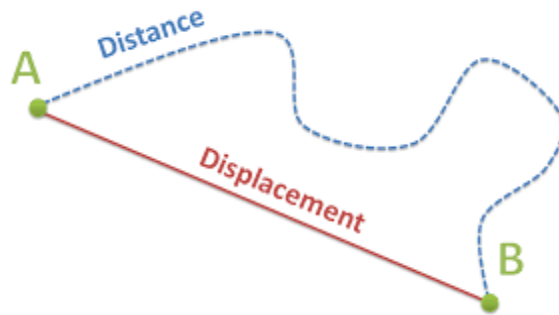
Velocity: The rate at which position changes (basically speed with direction)

Displacement: Distance and direction from the starting point (ex: 30 meters 10° west)

*Speed* how fast you are travelling



*Velocity* "speed in a given direction"



<https://www.coolkidfacts.com/speed-and-velocity/> <http://thescienceclassroom.org/physics/motion-in-1-d/distance-and-displacement/>

### Example Problems:

(1) Finding distance given speed and time

Avg. speed= 70 mi/hr

Time= 14 hours

Distance= ?

### How to solve:

Equation: Average speed=(distance)/(time)

Rearrange equation: distance=(avg speed)(time)

Substitute: distance=(70)(14)

Final Answer: distance=980 miles

(2) Finding time given speed and distance

Avg. speed: 75 mi/hr  
 Distance: 360 mi  
 time= ?

$$\text{time} = (\text{distance}) / (\text{avg. speed}) = (360) / (75) = \underline{4.8 \text{ hrs}}$$

(3) Word problem using travel in 2 directions

You travel at 30 meters per second east for 4 seconds and then 50 m/s west for 3 seconds. What is the average speed? What is the average velocity?

Tip: when tackling word problems underline all the numbers given to you and then write them out with what unit of measurement that number represents. This makes it easier to figure out which equation is best to use. In the case of two different directions using two different colors to differentiate between numbers can also be helpful.

Travel in the East Direction

Speed=30 m/s  
 Time= 4 seconds

$$\text{distance} = (30)(4) = 120 \text{ meters}$$

Travel in the West Direction

Speed= 50 m/s  
 Time= 3 seconds

$$\text{distance} = (50)(3) = 150 \text{ meters}$$

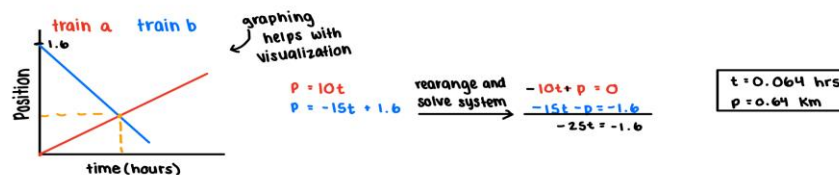
$$\text{Average speed} = (\text{total distance}) / (\text{total time}) = (120+150) / (7) = \underline{38.57 \text{ m/s}}$$

$$\text{Average velocity} = (\text{displacement}) / (\text{total time}) = (120-150) / (7) = \underline{-4.3 \text{ m/s or } 4.3 \text{ m/s west}}$$

\*\*when finding the displacement think of the east direction as positive and the west direction as negative

(4) Word problem using two objects traveling in different directions

Two trains are 1600 meters apart and heading toward one another. Train A is headed north at 10 km/hr while train B is headed south at 15 km/hr Where and when will they collide?



# 1 Dimensional Motion

## Acceleration

Acceleration: The rate of change of velocity (every second it gains x amount of speed)

Equation:  $\text{acceleration} = (\text{change in velocity}) / (\text{time})$

Example: 0-60 mi/hr in 4 seconds

$\text{acceleration} = (\text{change in velocity}) / (\text{time}) = (60-0) / (4) = 15 \text{ (mi/hr)/(s)}$

(every second it gains 15 mi/hr)

Kinematic Equations -have these memorized!

$\text{final velocity} = \text{initial velocity} + (\text{acceleration})(\text{time})$

$\text{displacement} = (\text{initial velocity})(\text{time}) + (1/2)(\text{acceleration})(\text{time}^2)$

$\text{final velocity}^2 = \text{initial velocity}^2 + (2)(\text{acceleration})(\text{distance})$

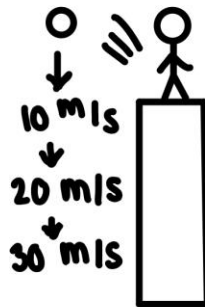
More pointers about displacement, velocity, and acceleration

1. When displacement is positive, the object is to the right of zero (or above zero)
2. When velocity is positive, the object is heading to the right of zero (or up)
3. If acceleration is positive, the force is to the right or upwards (\*\*force is a push or pull)

### Free Fall

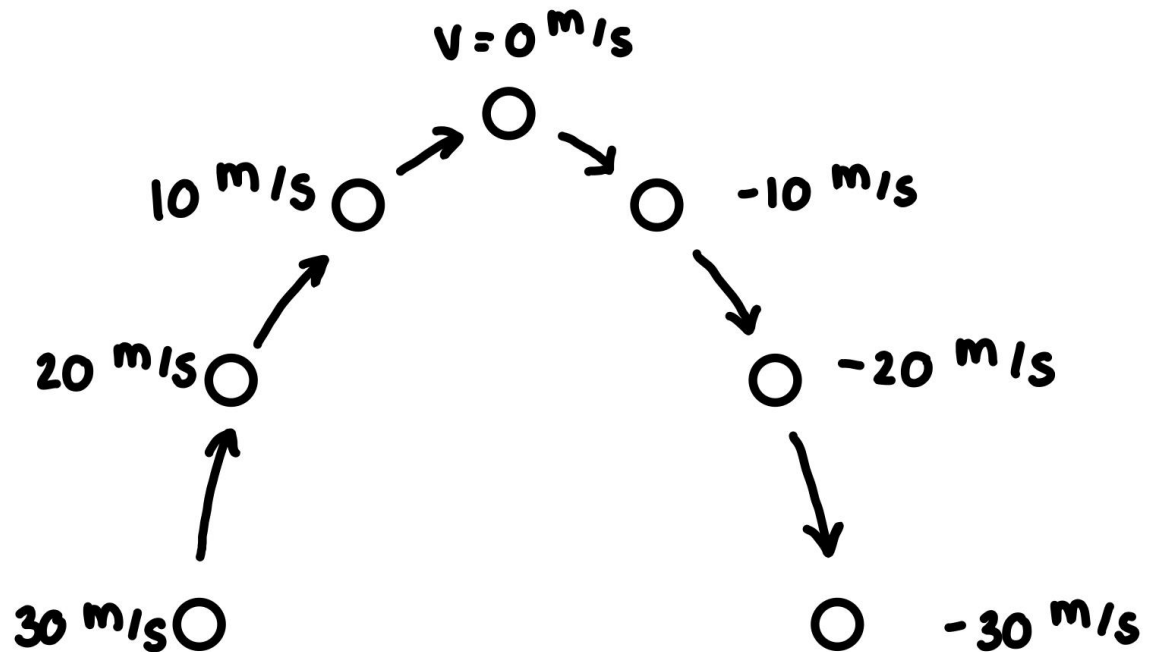
- Objects fall under the influence of gravity alone
- Any object, regardless of weight accelerate at the same rate
- Freefall rate of acceleration: 9.8  
m/s<sup>2</sup>

Acceleration due to gravity =  $-9.8 \text{ m/s}^2$



the ball gains  $\approx 10 \text{ m/s}$   
of speed every second

## The Ball in the Air Problem



- (1) How fast was the ball thrown? (it took 1.8 seconds for the ball to hit the ground after thrown)

Equation: final velocity = initial velocity + (acceleration)(time)

How to go about solving: Cut the time in half so that you can solve using the amount of time it took for the ball to get to the top. At the top, the velocity of the ball is 0, so that can be used as the final velocity.

$$0 = (\text{initial velocity}) + (-9.8)(.9) \rightarrow \underline{\text{initial velocity} = 8.82 \text{ m/s}}$$

- (2) How high did the ball go?

Equation: displacement = (initial velocity)(time) +  $(\frac{1}{2})(\text{acceleration})(\text{time}^2)$

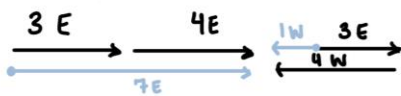
How to go about solving: since we have all of the values needed to plug into the equation we would just have to substitute to solve for the displacement, or in this case; height.

$$\text{displacement} = (8.82)(.9) + (\frac{1}{2})(9.8)(.9)^2 \rightarrow \underline{\text{height} = 3.969 \text{ m}}$$

## 2 Dimensional Motion

<u>Vector:</u> magnitude and direction	velocity	displacement	acceleration	force
<u>Scalar:</u> magnitude only	volume	mass	speed	length

*m = resultant*



*tan θ = 4/3*  
*θ = tan<sup>-1</sup>(4/3)*  
*θ = 53°*

*tan θ = 3/4*  
*θ = tan<sup>-1</sup>(3/4)*  
*θ = 37°*

*\* put calculator in degree mode*

Equations for Projectiles:

$$X = V_x t$$

horizontal distance      horizontal velocity  
↑                                      ↑  
time

$$V_y = V_{y0} + gt$$

vertical velocity      initial vertical velocity      -9.8  
↑                                      ↑                                      ↑  
time

$$y = V_{y0} t + \frac{1}{2} gt^2$$

vertical distance      time                                      -9.8  
↑                                      ↑                                      ↑  
initial vertical velocity      time

## Vectors

Rules for vector addition:

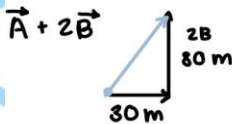
1. Place vectors tail to tip
2. Draw resultant from open tail to open tip
3. Report magnitude and direction

vector A

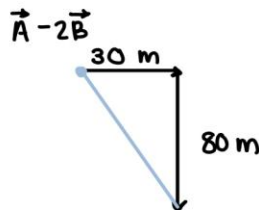
$$\vec{A} = 30 \text{ m E}$$

$$\vec{B} = 40 \text{ m N}$$

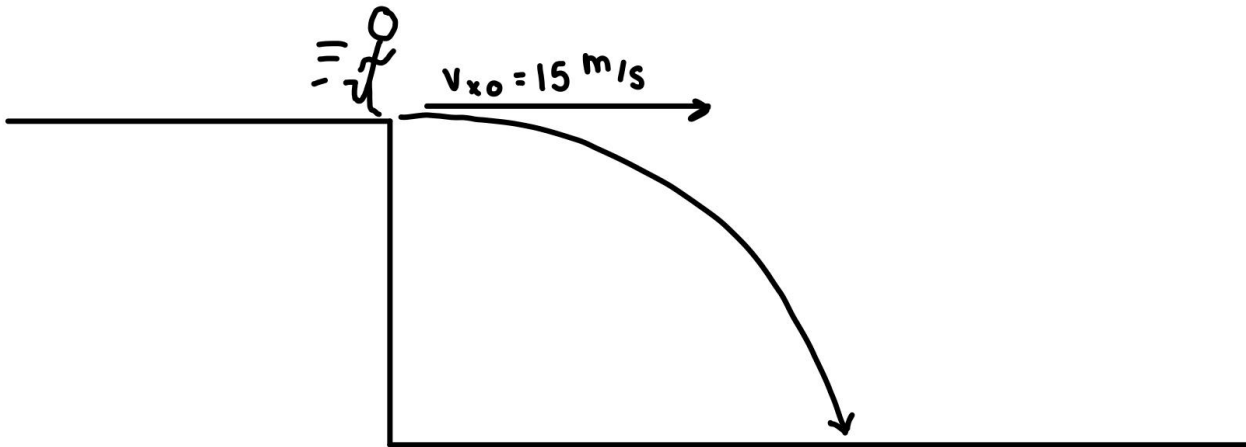
Find  $\vec{A} + \vec{B}$     50 m @ 53°  
 $\tan^{-1}(\frac{40}{30})$



$30^2 + 80^2 = c^2$   
 $c = 85.44$   
 $\tan^{-1}(80/30) = 69.4^\circ$



Examples

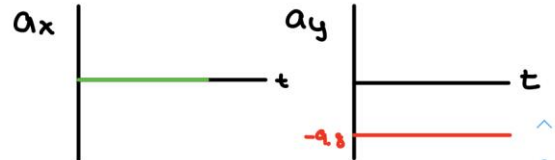
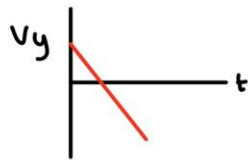
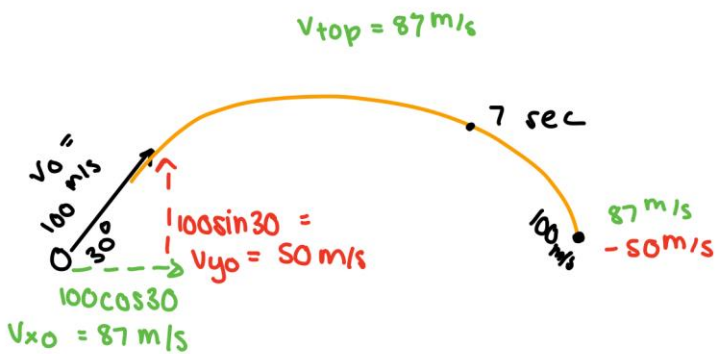


how far from the base of the cliff does he land?

$$y = \frac{1}{2} g t^2 \rightarrow t = \sqrt{\frac{2y}{g}} = \sqrt{\frac{2(-25)}{-9.8}} = 2.26 \text{ sec}$$

$$x = v_x t \rightarrow x = (15 \text{ m/s})(2.26 \text{ sec}) = \boxed{33.9 \text{ m}}$$

Upwardly Launched Projectiles:



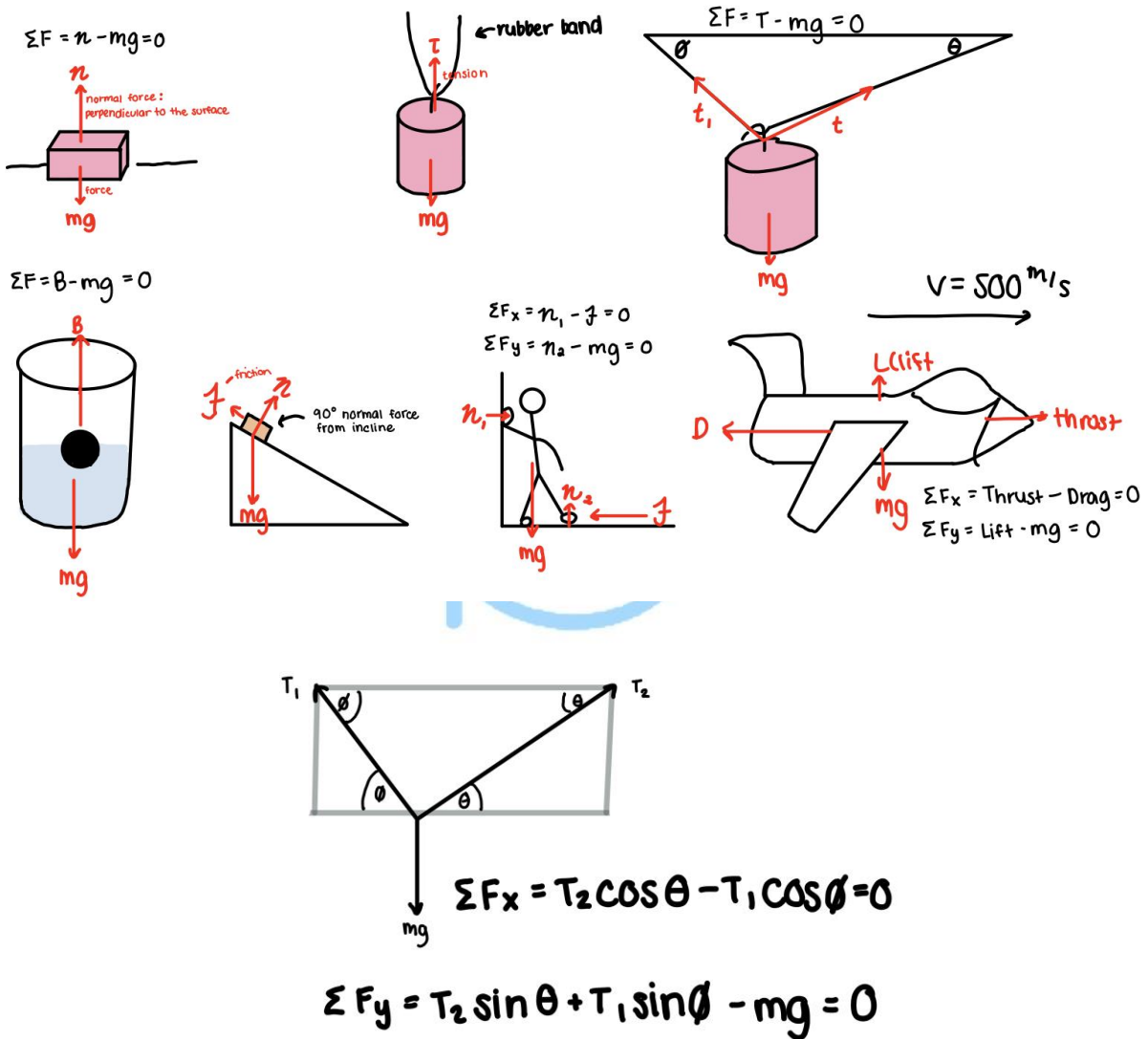


# Newton's Laws

Force: push or pull

- Unit: Newtons (N)
  - Mass: amount of matter (kg)
  - Volume: amount of space (m<sup>2</sup>)
  - Weight: force due to gravity (N)
    - weight=(mass)(9.8)

Drawing Freebody Diagrams:



Newton's First Law: If the sum of the forces (net force)=0, then the acceleration=0

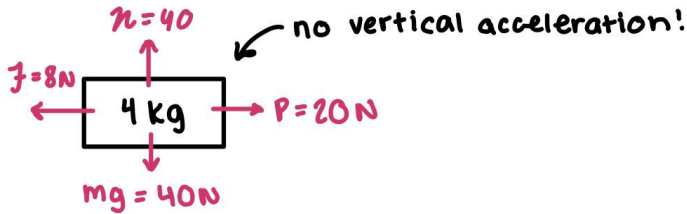
Inertia: Resistance to a change in motion (dependent on mass)

- Larger mass = larger inertia

Newton's Second Law: If the net force doesn't equal zero, the acceleration doesn't equal zero

$$\sum F_x = P - J = ma \rightarrow 20 - 8 = 4a \quad a = 3 \text{ m/s}^2$$

$$\sum F_y = n - mg = 0 \rightarrow n = mg = 40 \text{ N}$$



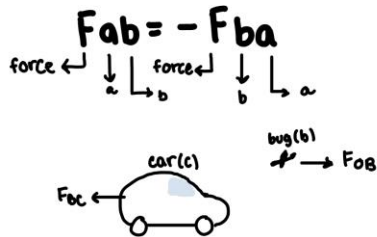
IF  $M \uparrow$  THEN  $A \downarrow$  ( $a \propto \frac{1}{m}$ )

$$a = \frac{\sum F}{m}$$

$$\sum F = ma$$

$$T - mg = ma$$

Newton's Third Law: For every action there is an equal and opposite reaction.

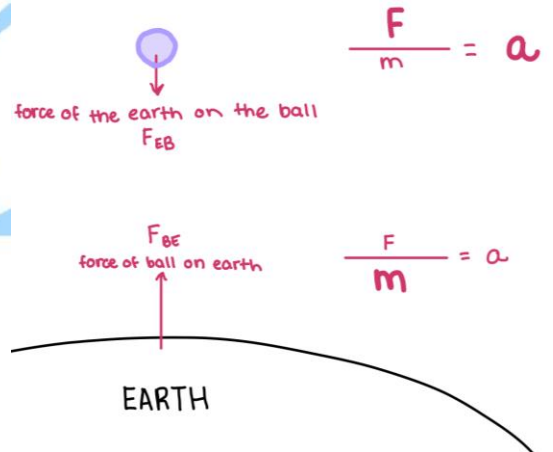


$$F_{ab} = -F_{ba}$$

$$\frac{F}{\text{MASS}} = a$$

$$\frac{F}{\text{MASS}} = a$$

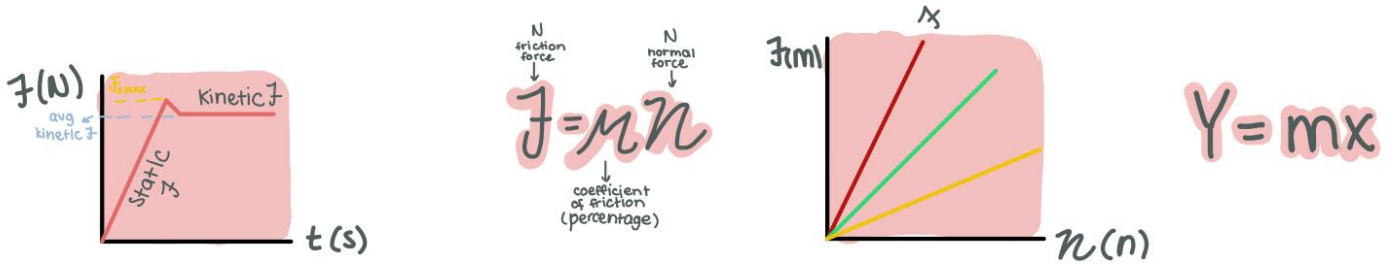
Same force, different acceleration!



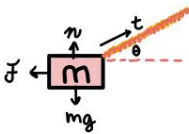
$$\frac{F}{m} = a$$

$$\frac{F}{m} = a$$

## Friction



## Angled Forces

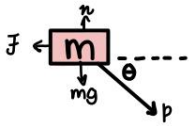


find acceleration:

$$\begin{cases} \Sigma F_y = n - mg + T \sin \theta = 0 \\ \Sigma F_x = T \cos \theta - f_k = ma \end{cases}$$

$$\begin{cases} T \cos \theta - \mu_k n = ma \\ n = mg - T \sin \theta \\ T \cos \theta - \mu (mg - T \sin \theta) = ma \end{cases}$$

$$m = \frac{T \cos \theta - \mu (mg - T \sin \theta)}{a}$$

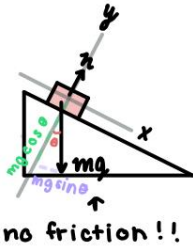


find acceleration:

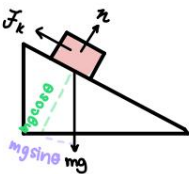
$$\begin{cases} \Sigma F_y = n - mg + P \sin \theta = 0 \\ \Sigma F_x = P \cos \theta - f_k = ma \end{cases}$$

$$\begin{cases} P \cos \theta - \mu n = ma \\ P \cos \theta - \mu (mg + P \sin \theta) = ma \end{cases}$$

$$a = \frac{P \cos \theta - \mu (mg + P \sin \theta)}{m}$$

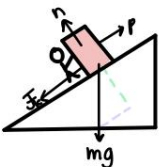


$$\begin{aligned} \Sigma F_y = n - mg \cos \theta &= 0 \Rightarrow n = mg \cos \theta \\ \Sigma F_x = mg \sin \theta &= ma \\ a &= g \sin \theta \end{aligned}$$



$$\begin{aligned} \Sigma F_y = n - mg \cos \theta &= 0 \\ \Sigma F_x = mg \sin \theta - f_k &= ma \end{aligned}$$

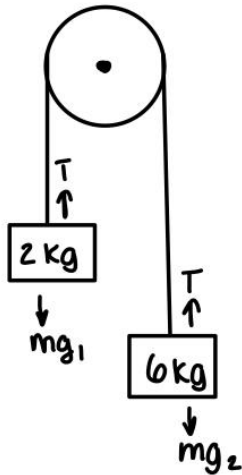
$$\begin{aligned} m \sin \theta - \mu n &= ma \\ a &= \frac{g \sin \theta - \mu (g \cos \theta)}{m} \end{aligned}$$



$$\begin{aligned} \Sigma F_y = n - mg \cos \theta &= 0 \\ \Sigma F_x = P - f_k - mg \sin \theta &= ma \end{aligned}$$

$$\begin{aligned} P - \mu n - mg \sin \theta &= ma \\ a &= \frac{P - \mu mg \cos \theta - mg \sin \theta}{m} \end{aligned}$$

Atwood Machine Examples:



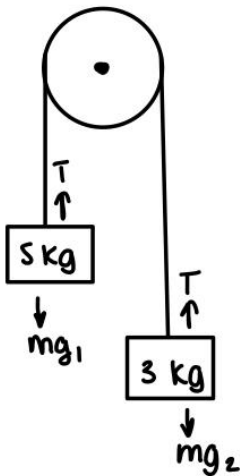
$$\Sigma F_2 = T - mg_1 = ma$$

$$\hookrightarrow T - 20 = 2a$$

$$\Sigma F_6 = mg_2 - T = ma$$

$$\hookrightarrow 60 - T = 6a$$

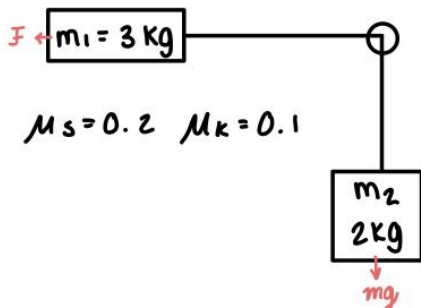
$$\begin{array}{r} T - 20 = 2a \\ 60 - T = 6a \\ \hline 40 = 8a \\ a = 5 \text{ m/s}^2 \\ T = 30 \text{ N} \end{array}$$



$$\Sigma F_{\text{system}} = m_5 g - m_3 g = (m_3 + m_5) a$$

$$50 - 30 = 8a$$

$$a = 2.5$$



$$\mu_s = 0.2 \quad \mu_k = 0.1$$

$$\Sigma F_1 = T - F_k = m_1 a$$

$$= T - \mu_k n = m_1 a$$

$$= T - \mu_k m_1 g = m_1 a$$

$$= T - (0.1)(30) = 3a$$

$$T - 3 = 3a$$

$$\Sigma F_2 = 20 - T = 2a$$

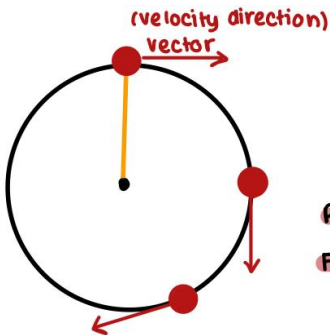
$$\begin{array}{r} T - 3 = 3a \\ 20 - T = 2a \\ \hline 17 = 5a \\ a = 3.4 \text{ m/s}^2 \\ T = 13.2 \text{ N} \end{array}$$

Quick way:

$$\Sigma F_{\text{system}}: 20 - 3 = 5a$$

$$a = 3.4 \text{ m/s}^2$$

# Circular Motion



$$\text{velocity } \frac{\text{m/s}}{V} = \frac{2\pi r}{T}$$

radius  
time for 1 circle (sec)

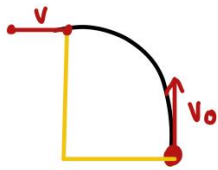
Period: time for 1 circle

Frequency: # of circles per second

} inverse relationship

$$T = 1/f$$

$$f = 1/T$$



$$a = \frac{\Delta v}{t} = \frac{v - v_0}{t} = \frac{v_0 \sqrt{2}}{t} = \text{acceleration}$$

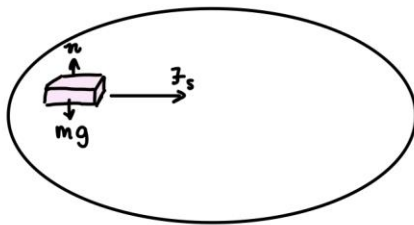
centripetal = inward

$$a_c = \frac{v^2}{r} \rightarrow \text{amount of acceleration}$$

$$F_c = \frac{mv^2}{r}$$

$$v = \frac{2\pi r}{T} \quad T = 1/f \quad f = 1/T \quad a_c = \frac{v^2}{r} \quad F_c = \frac{mv^2}{r}$$

## Friction during circular motion:



$$\sum F_y = n - mg = 0 \quad n = mg$$

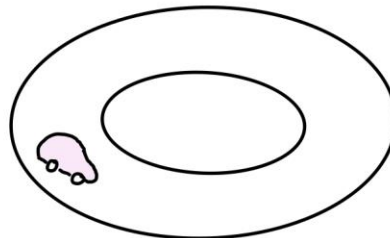
$$\sum F_c = F_s = (m) \left( \frac{v^2}{r} \right) \quad \mu_s n = \frac{mv^2}{r}$$

$$\mu_s mg = \frac{mv^2}{r}$$

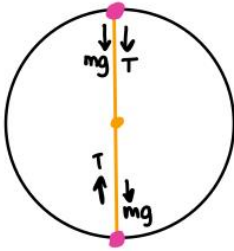
$$v = \sqrt{r\mu g}$$

↑  
max. speed

$$v_{\max} = \sqrt{r\mu g} \rightarrow \mu = \frac{v^2}{rg}$$



## Vertical Circles



$$\Sigma F_c = T + mg = \frac{mv^2}{r} \quad T = \frac{mv^2}{r} - mg$$

$$\Sigma F_c = T - mg = \frac{mv^2}{r} \quad T = \frac{mv^2}{r} + mg$$

$$n = \frac{mv^2}{r} = mg$$

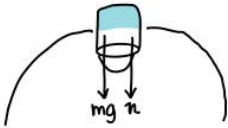
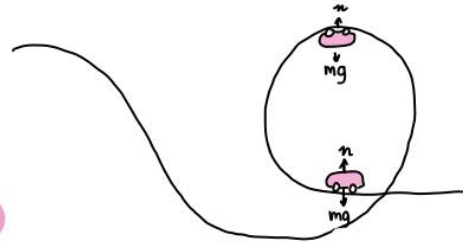
$$n - mg = \frac{mv^2}{r}$$

$$n = \frac{mv^2}{r} + mg$$

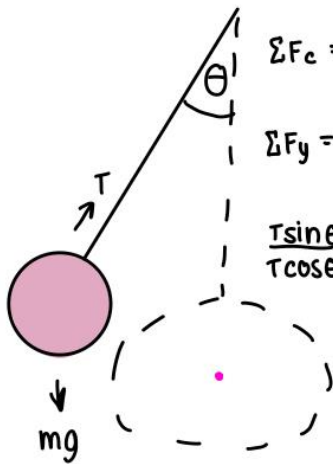
minimum speed to complete a circle ( $v_{min}$ )

$$T + mg = \frac{mv^2}{r}$$

@  $v_{min}$   $T$  approaches zero  $\cancel{T} + mg = \frac{mv^2}{r} \rightarrow v_{min} = \sqrt{gr}$



← don't go less than the  $\sqrt{gr}$ !



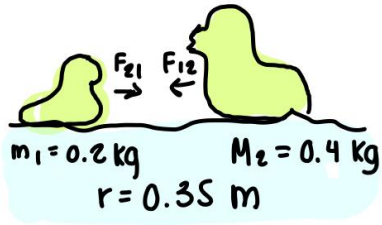
$$\Sigma F_c = T \sin \theta = \frac{mv^2}{r} \rightarrow T \sin \theta = mg$$

$$\Sigma F_y = T \cos \theta - mg = 0$$

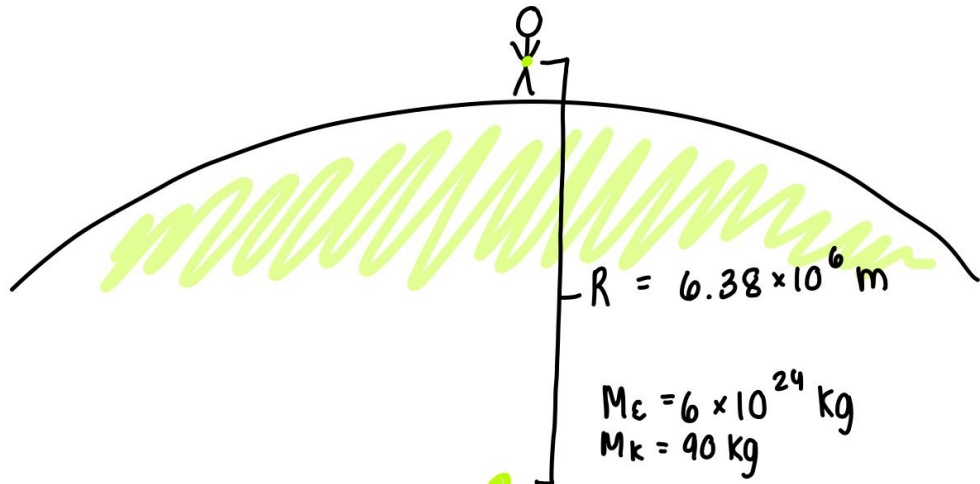
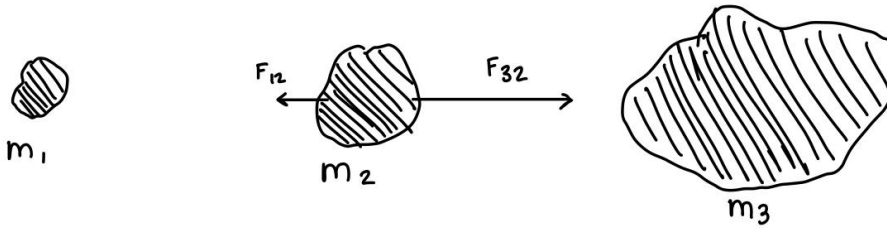
$$\frac{T \sin \theta}{T \cos \theta} = \frac{\frac{mv^2}{r}}{mg}$$

$$\tan \theta = \frac{v^2}{rg}$$

## Gravity

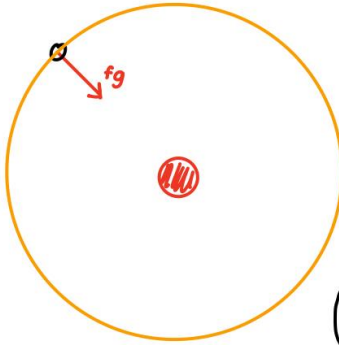


$$\begin{aligned}
 & 6.67 \times 10^{-11} \frac{\text{Nm}^2}{\text{kg}^2} \\
 & \rightarrow F = \frac{G m M}{r^2} \\
 & = \frac{(6.67 \times 10^{-11})(0.2)(0.4)}{0.35^2} = 4.36 \times 10^{-11} \text{ N}
 \end{aligned}$$



$$F = \frac{G m M}{r} \Rightarrow mg = \frac{G m M}{r^2} = \frac{(6.67 \times 10^{-11})(6 \times 10^{24})}{6.38 \times 10^6} = 9.8$$

# Kepler's Third Law

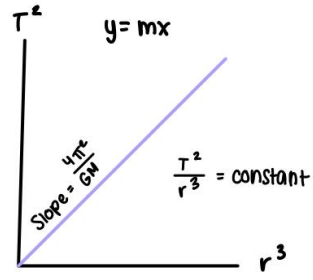


$$\Sigma F_c = \frac{GMm}{r^2} = \frac{mv^2}{r}$$

$$v = \frac{2\pi r}{t}$$

$$\frac{GMm}{r^2} = m \left( \frac{2\pi r}{t} \right)^2 \frac{1}{r}$$

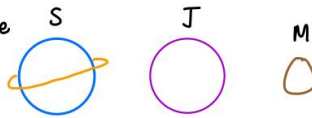
$$\frac{GM}{r^2} = \frac{4\pi^2 r^2}{T^2 r}$$



$$T^2 = \left( \frac{4\pi^2}{GM} \right) r^3 \leftarrow \text{Kepler's 3rd law}$$

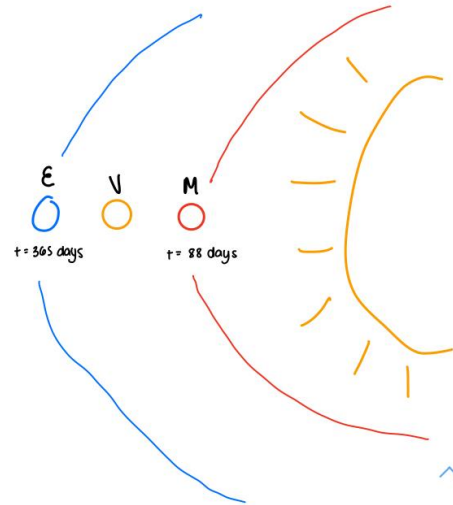
$$\frac{t_e^2}{r_e^3} = \frac{t_m^2}{r_m^3}$$

r = distance from the sun



$$\frac{365^2}{93^3} = \frac{88^2}{r_m^3} \quad r_m = 36.03 \text{ mm}$$

$$\frac{t_e^2}{r_e^3} = \frac{t_n^2}{r_n^3} \quad \frac{365^2}{93^3} = \frac{60190^2}{r_n^3} \quad r_n = 2797 \text{ mm}$$





# Work and Energy

energy: the ability to do work

work: force  $\times$  distance

work  
newton-meter  
joule

$$W = Fd \cos \theta$$

force (N) distance (m)  
angle between force and d

$$\sum F_x = T \cos \theta - F_k = ma$$

$$150 \cos 30 - (0.2)(317) = 40a$$

$$a = 1.66 \text{ m/s}^2$$

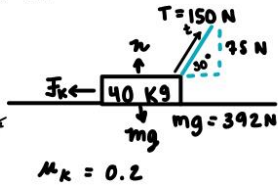
$$v^2 = v_0^2 + 2ad$$

$$v = 4.82 \text{ m/s}$$

$$W = \Delta E$$

$$445 \text{ J} = \frac{1}{2}(40)v^2 - \frac{1}{2}(40)(0)^2$$

$$v = 4.82 \text{ m/s}$$



calculate the work done by each force:

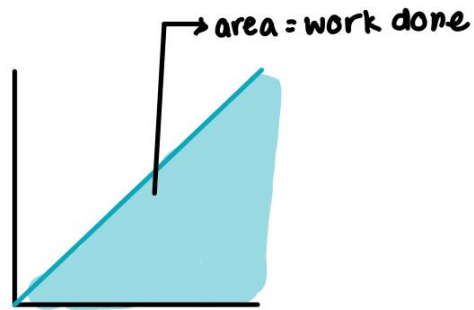
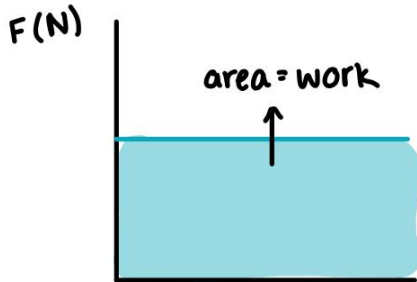
$$W_{\text{tension}} = Td \cos \theta = (150 \text{ N})(7 \text{ m}) \cos 30^\circ = 909 \text{ J}$$

$$W_{mg} = (mg)d \cos \theta = (40 \text{ kg})(9.8 \text{ m/s}^2) \cos 90^\circ = 0 \text{ J}$$

$$W_{F_k} = F_k d \cos \theta = (\mu_k N)d \cos \theta = (0.2)(317 \text{ N})(7 \text{ m}) \cos 180^\circ = -444 \text{ J}$$

$$W_N = Nd \cos \theta = 0 \text{ J}$$

$$W_{\text{NET}} = 909 + 0 + (-444) + 0 = 465 \text{ J}$$



d(m)

## Types of Energy

kinetic energy: the energy of motion

$$K_E = \frac{1}{2}mv^2$$

kinetic energy (J) mass (kg) speed (m/s)

potential energy (gravitational): energy of position (height)

$$P_E = mgh$$

mass (kg) height (m)

potential energy (elastic): energy of position (stretch)

$$P_E = \frac{1}{2}kx^2$$

spring constant (N/m) stretch (m)

## Work Energy Theorem

$$W = \Delta E$$

$$W = \frac{1}{2}mv^2 - \frac{1}{2}mV_0^2$$

$$W = mgh - mgh_0$$

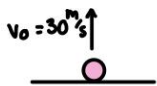
$$W = \frac{1}{2}kx^2 - \frac{1}{2}kx_0^2$$

## Conservation of Energy

$$PE_0 + KE_0 = PE + KE$$

$$U_0 + K_0 = U + K$$

Ex 1.  $v = 0$



Find the max height:

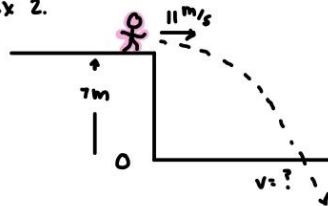
$$U_0 + K_0 = U + K$$

$$\frac{1}{2}mv^2 = mgh$$

$$\frac{1}{2}(30)^2 = (9.8)h$$

$$h = 45.9 \text{ m}$$

Ex 2.



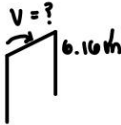
$$U_0 + K_0 = U + K$$

$$mgh_0 + \frac{1}{2}mv^2 = \frac{1}{2}mv^2$$

$$(9.8)(7) + \frac{1}{2}(11^2) = \frac{1}{2}v^2$$

$$v = 16.1 \text{ m/s}$$

Ex 3



$$U_0 + K_0 = U + K$$

$$\frac{1}{2}mv_0^2 = mgh + \frac{1}{2}mv^2$$

$$\frac{1}{2}(7^2) = (9.8)(6.10) + \frac{1}{2}(v^2)$$

$$24.5 = 60.4 + \frac{1}{2}v^2 \text{ not possible (too slow)}$$

How fast does he have to run?

$$K_0 + U_0 = K + U$$

$$\frac{1}{2}mv_0^2 = mgh$$

$$\frac{1}{2}(v_0^2) = (9.8)(6.10)$$

$$v_0 = 11 \text{ m/s}$$

## Power

anytime rate is mentioned think **POWER**  $R = \frac{\text{change of position}}{\text{time}}$

$$P = \frac{W}{t}$$

$\downarrow$  power (watt)      $\downarrow$  time (sec)

$$P = \frac{\Delta E}{t}$$

$$P = \frac{mgh - mgh_0}{t}$$

$$P = \frac{\frac{1}{2}mv^2 - \frac{1}{2}mV_0^2}{t}$$

$$P = \frac{Fd}{t}$$

$$P = F\bar{V}$$

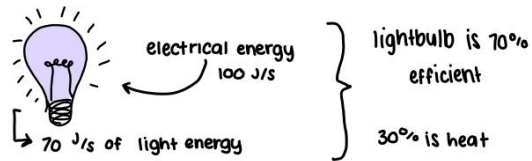
$\swarrow$  avg. speed

$t = 2 \text{ seconds}$

$$P = \frac{W}{t} = \frac{Fd \cos \theta}{t} = \frac{(40)(3)}{2} = 60 \text{ watts}$$

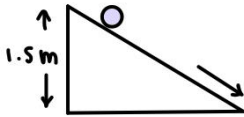
## Efficiency

$$\text{efficiency} = \frac{\text{energy out}}{\text{energy in}} \times 100$$

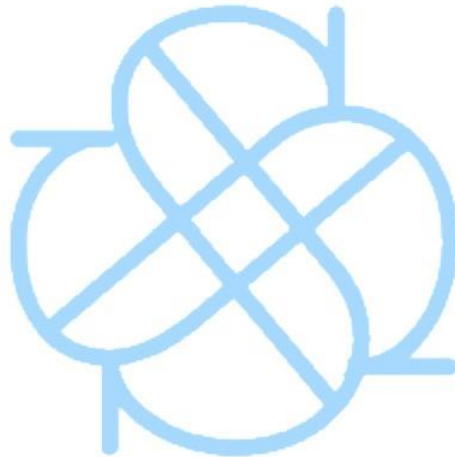


Example: A 3 kg ball rolls down a 1.5 m high hill, it reaches a speed of 4.3 m/s.  
What was the efficiency of the energy transfer?

Heat



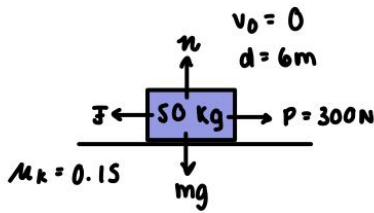
$$\text{eff} = \frac{\text{energy out}}{\text{energy in}} = \frac{\frac{1}{2}mv^2}{mgh} = \frac{(\frac{1}{2})(3)(4.3)^2}{(3)(9.8)(1.5)} \times 100 = 62.8\% \text{ eff}$$



$$|W_f| = \text{heat}$$

$$\mu n d = \text{heat}$$

$$W_f + U_o + K_o = U + K + \text{heat}$$



$$W = F d \cos \theta$$

$$W_P = (300)(6) \cos 0 = 1800 \text{ J}$$

$$W_{mg} = (490)(6) \cos 90 = 0$$

$$W_n = 0$$

$$W_f = (\mu n) d \cos \theta = (0.15)(490)6 \cos 180 = -441 \text{ J}$$

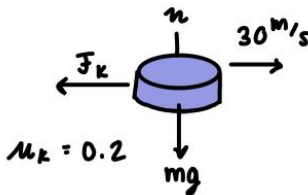
$$W_{\text{NET}} = 1359 \text{ J}$$

$$W_f + U_o + K_o = U + K + \text{heat}$$

$$1800 = K + 441$$

$$K = 1359 \text{ J}$$

Ex 1:



Question: How far does it slide before coming to rest?

$$W_f + U_o + K_o = U + K + \text{heat}$$

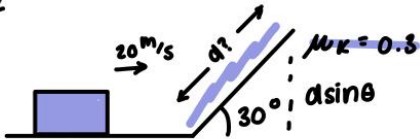
$$\frac{1}{2} m v_o^2 = \mu n d$$

$$\frac{1}{2} m v_o^2 = \mu m g d$$

$$\left(\frac{1}{2}\right)(30^2) = (0.2)(9.8)d$$

$$d = 229.6 \text{ m}$$

Ex 2



$$W_f + U_o + K_o = U + K + \text{heat}$$

$$\frac{1}{2} m v_o^2 = mgh + \mu m g \cos \theta d$$

$$\left(\frac{1}{2}\right)(20^2) = (9.8)(d \sin \theta) + (0.3)(9.8 \cos 30)(d)$$

$$200 = (9.8)(d \sin \theta) + 2.55d$$

$$200 = d(9.8 \sin 30 + 2.55)$$

$$d = 26.8 \text{ m}$$

Ex 3

How much heat is produced?



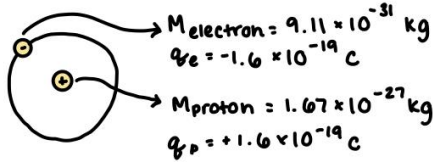
$$W_f + U_o + K_o = U + K + \text{heat}$$

$$\left(\frac{1}{2}\right)(3)(10^2) + \left(\frac{1}{2}\right)(6)(5^2) = \text{heat}$$

$$\text{heat} = 225 \text{ J}$$

# Electric Currents and Magnetism

## Electricity



$6.25 \times 10^{18} \text{ e's} \Rightarrow -1 \text{ coulomb}$   
 $6.25 \times 10^{18} \text{ p's} \Rightarrow +1 \text{ coulomb}$   
 $\downarrow$  micro coulomb  
 $1 \mu\text{C} = 1 \times 10^{-6} \text{ C}$   
 $5 \mu\text{C} = 5 \times 10^{-6} \text{ C}$

Opposite charges attract

Like charges repel



Coulomb's Law

$$F = \left| \frac{k q_1 q_2}{r^2} \right|$$

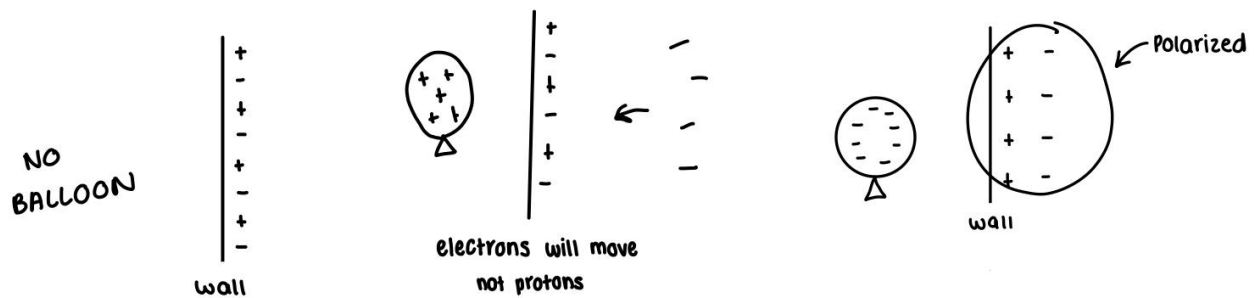
$F = \text{force (N)}$   
 $k = 9 \times 10^9 \left( \frac{\text{Nm}^2}{\text{C}^2} \right)$

$q_1 =$  charge (C)  
 $q_2 =$  charge (C)

$r =$  distance between charges (m)

Find the force  $q_1$  has on  $q_2$

$$F = \left| \frac{k \cdot q_1 \cdot q_2}{r^2} \right| = \left| \frac{(9 \times 10^9)(3.2 \times 10^{-19})(1.6 \times 10^{-19})}{(0.35)^2} \right| = 3.76 \times 10^{-27} \text{ N} \leftarrow$$



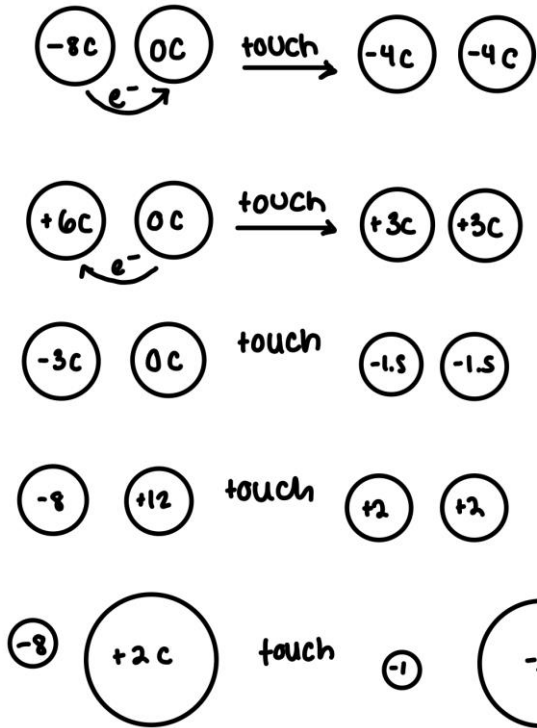
**Conduction:** material in which electrons tend to be free and therefore rearrange and flow easily.

**Insulator:** material in which electrons do not tend to be free and therefore do not rearrange and flow easily.

# Methods of Charging

Conduction → "touch"  
near

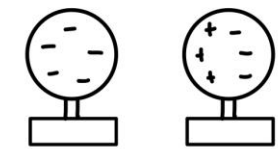
Induction → no touch-bring



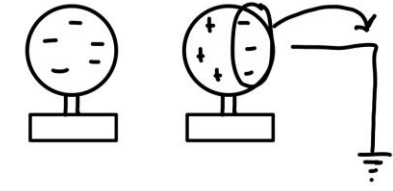
t = 0



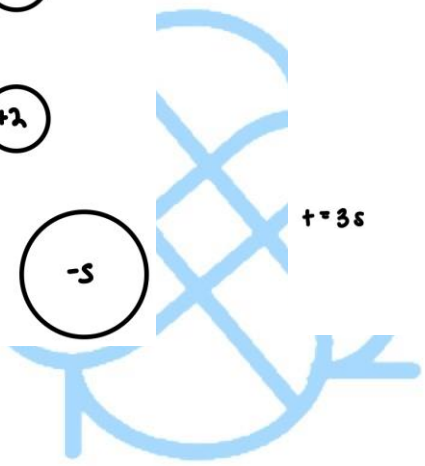
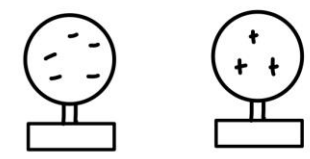
t = 1 s



t = 2 s



t = 3 s

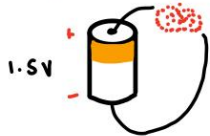


## Current Electricity

$$\text{Ohm's Law: } I = \frac{V}{R}$$

R = resistance  $1 \Omega$  unit: ohm =  $1 \frac{V}{A}$   
↳ opposition to flow

V = voltage  $1 \text{ volt} = 1 \frac{J}{C}$

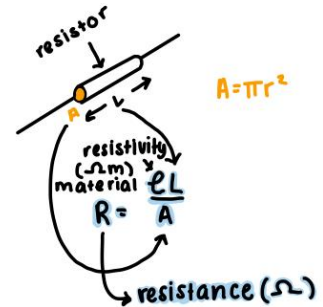


I = current  
↳ flow of charge

unit:  $1 \text{ Amp} = 1 \frac{C}{s}$

$$I = \frac{Q}{t}$$

$$\hookrightarrow Q = It$$



If V goes  $\uparrow$ , then the current (I) goes  $\downarrow$   $I \propto V$

If R goes  $\uparrow$  then I goes  $\downarrow$   $I \propto \frac{1}{R}$

## Equation for Power

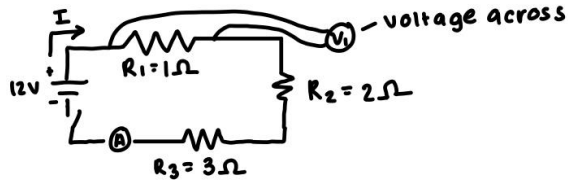
↳ voltage (V)

$$P = VI$$

↳ power (watt)

↳ current (A)

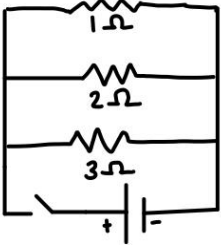
## Series Circuits



### Rules + Example

- ①  $R_{total} = R_1 + R_2 + R_3 = 1 + 2 + 3 = 6\Omega$
- ②  $I_{total} = \frac{V_t}{R_t} = \frac{12}{6} = 2 \text{ amps}$
- ③  $V_1 = IR_1 = (2)(1) = 2 \text{ volts of electrical pressure through } R_1$
- ④  $V_T = V_1 + V_2 + V_3 = 2v + 4v + 6v = 12V$

## Parallel Circuits



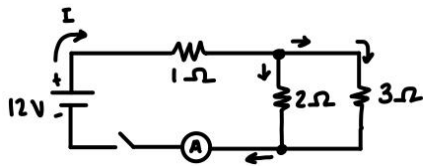
### Rules:

- ①  $R_T = (R_1^{-1} + R_2^{-1} + R_3^{-1})^{-1}$   
 $= (1^{-1} + 2^{-1} + 3^{-1})^{-1} = 0.545\Omega$
- ②  $I_t = \frac{V_T}{R_T} = \frac{12}{0.545} = 22 \text{ amps}$
- ③  $V_T = V_1 = V_2 = V_3$

$$\textcircled{4} \begin{aligned} I_1 &= \frac{V}{R_1} \\ I_2 &= \frac{V}{R_2} \\ I_3 &= \frac{V}{R_3} \end{aligned}$$

- ⑤  $I_T = I_1 + I_2 + I_3$  ← kirchoffs loop rule  
 conservation of energy

## Combination Circuits

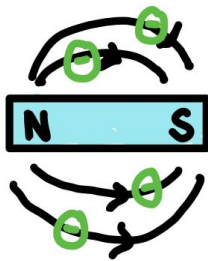


### Rules:

- ①  $R_T = (2^{-1} + 3^{-1})^{-1} + 1 = 2.2\Omega$
- ②  $I_t = \frac{V_t}{R_T} = \frac{12}{2.2} = 5.45 \text{ amps}$
- ③  $V_{drop}$  across mainline resistors:  $V_1 = IR_1 = (5.45)(1\Omega) = 5.45 \text{ V}$
- ④ find leftover voltage:  $12V - 5.45V = 6.55V$  ← for parallel part

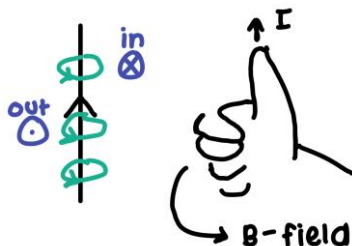
## Magnetic Forces

There is a magnetic field that goes from the north to south field



## The Right Hand Rule

This video provides some great examples of the right hand rule as it is a difficult concept to understand without being talked through it: <https://www.youtube.com/watch?v=IKEt5bvn7LU>



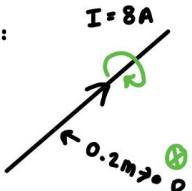


## Calculating the magnitude of the magnetic field


$$B = \frac{\mu_0 I}{2\pi r}$$

$4\pi \times 10^{-7} \frac{Tm}{A}$  (pointing to  $\mu_0$ )  
 $\mu_0$  (pointing to  $4\pi \times 10^{-7}$ )  
 $I$  (pointing to  $I$ ) → current (A)  
 $2\pi r$  (pointing to  $r$ ) → distance (m)  
 $B$  (pointing to  $B$ ) → Magnetic Field (Tesla)

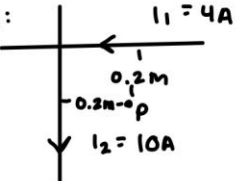
Ex 1:



$$B = \frac{\mu_0 I}{2\pi r} = \frac{(4\pi \times 10^{-7})(8)}{2\pi(0.2)} = 8 \times 10^{-6} \text{ teslas (T)}$$

$8 \times 10^{-6} \text{ T}$   


Ex 2:

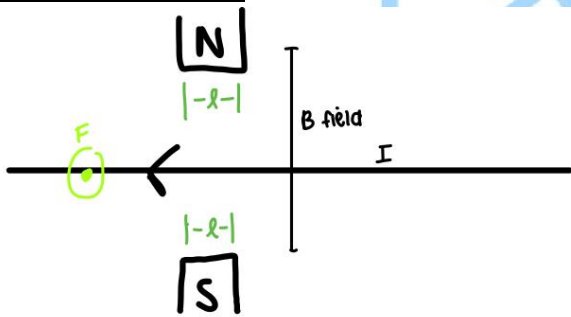


$$B = \frac{(4\pi \times 10^{-7}) 4}{2\pi(0.2)} = 4 \times 10^{-6} \text{ T } \odot$$

$$B = \frac{(4 \times 10^{-7}) 10}{2\pi(0.2)} = 1 \times 10^{-5} \text{ T } \odot$$

$$(4 \times 10^{-6}) + (1 \times 10^{-5}) = \boxed{10 \times 10^{-6} \text{ T } \odot}$$

## Magnetic Forces



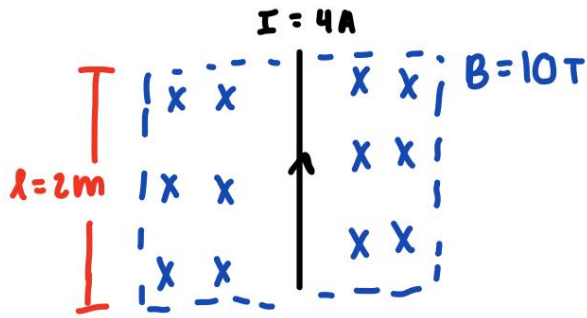
$$F = B I l \sin\theta$$

$\downarrow$  N     $\downarrow$  (T)     $\downarrow$  (A)     $\downarrow$  (m)     $\swarrow$  angle between B and I

$$F = B v q \sin\theta$$

$\downarrow$  N     $\downarrow$  (T)     $\downarrow$  (m/s)     $\downarrow$  (C)     $\downarrow$  dir B + v

## Example:



$$F = (10)(4)(2) \cos 90 = 80 \text{ N } \leftarrow$$